Formulas for PHY 141

| Kinematics |  |
| :---: | :---: |
| Constant acceleration | $\begin{aligned} & \mathbf{r}=\mathbf{r}_{0}+\mathbf{v}_{0} t+\frac{1}{2} \mathbf{a} t^{2} \\ & \mathbf{v}=\mathbf{v}_{0}+\mathbf{a} t \\ & v^{2}=v_{0}^{2}+2 \mathbf{a} \cdot\left(\mathbf{r}-\mathbf{r}_{0}\right) \end{aligned}$ |
| Circular motion | $\begin{aligned} & \mathbf{a}=\mathbf{a}_{r}+\mathbf{a}_{t} \\ & a_{r}=v^{2} / r=r \omega^{2} \\ & a_{t}=r \alpha, v=r \omega \end{aligned}$ |
| Dynamics |  |
| Gravity near earth's surface | $\mathbf{F}_{g}=m \mathbf{g}$ |
| Elastic force | $F=-k x$ |
| Friction | $\begin{aligned} & f_{k}=\mu_{k} N \\ & f_{s} \leq \mu_{s} N \end{aligned}$ |
| Effective gravity | $\mathbf{g}_{\text {eff }}=\mathbf{g}-\mathbf{a}$ |
| Potential Energy |  |
| Gravity near earth's surface | $U=m g y$ |
| Elastic force | $U=\frac{1}{2} k x^{2}$ |
| Rotational Motion |  |
| Circular motion vectors | $\mathbf{v}=\boldsymbol{\omega} \times \mathbf{r}$ |
| Radial acceleration | $\mathbf{a}_{r}=-\omega^{2} \mathbf{r}$ |
| Tangential acceleration | $\mathbf{a}_{t}=\boldsymbol{\alpha} \times \mathbf{r}$ |
| Moment of inertia (particle) | $I=m r^{2}$ |
| Rotational kinetic energy | $K_{\text {rot }}=\frac{1}{2} I \omega^{2}$ |
| Symmetric rigid body | $\begin{aligned} & \tau=I \boldsymbol{\alpha} \\ & L=I \omega \end{aligned}$ |


| Rolling | $\begin{aligned} v_{C M} & =R \omega \\ a_{C M} & =R \alpha \end{aligned}$ |
| :---: | :---: |
| Angular momentum (particle) | $\mathbf{L}=\mathbf{r} \times \mathbf{p}$ |
| Gravity and Satellite Motion |  |
| Point masses or spherically symmetric objects | $\begin{aligned} & F=G \frac{M m}{r^{2}} \\ & U=-G \frac{M m}{r} \end{aligned}$ |
| Planet with small satellite in orbit | $E=-G \frac{M m}{2 a}$ |
| Oscillations (SHM) |  |
| Displacement | $x=A \cos (\omega t+\phi)$ |
| Force | $F=-m \omega^{2} x$ |
| Potential Energy | $U=\frac{1}{2} m \omega^{2} x^{2}$ |
| Total energy | $E=\frac{1}{2} m \omega^{2} A^{2}$ |
| Mass on ideal spring | $\omega=\sqrt{k / m}$ |
| Wave Motion |  |
| Harmonic wave | $\begin{aligned} & y=A \cos (k x-\omega t+\delta) \\ & k=2 \pi / \lambda, \omega=2 \pi f \\ & v=f \lambda=\omega / k \end{aligned}$ |
| Interference, waves of equal intensity | $I=2 I_{0}(1+\cos \delta)$ |
| Phase difference due to path difference | $\delta=k \Delta x$ |
| Loudness level | $\beta=10 \log _{10}\left(I / I_{0}\right)$ |

Formulas for PHY 141

| Doppler effect, <br> source chasing <br> fleeing receiver | $f=f_{0} \frac{v-v_{R}}{v-v_{S}}$ |
| :--- | :---: |
| Standing wave, <br> string fixed at <br> both ends, pipe <br> open at both <br> ends | $f_{n}=n f_{1}, n=1,2,3, \ldots$ <br> $f_{1}=v / 2 L$ |
| Standing wave, <br> string fixed at <br> one end, pipe <br> open at one end | $f_{n}=n f_{1}, n=1,3,5, \ldots$ <br> $f_{1}=v / 4 L$ |
| Wave in string | $v=\sqrt{T / \mu}$ |
| Beat frequency | $f_{B}=\left\|f_{2}-f_{1}\right\|$ |


| Derivatives |  |
| :---: | :---: |
| Powers | $\begin{aligned} & \frac{d}{d x} x^{n}=n x^{n-1}, \\ & \frac{d}{d x} \ln x=\frac{1}{x} \end{aligned}$ |
| Exponentials | $\frac{d}{d x} e^{a x}=a e^{a x}$ |
| Trigonometry | $\begin{aligned} & \frac{d}{d x} \sin a x=a \cos a x \\ & \frac{d}{d x} \cos a x=-a \sin a x \end{aligned}$ |
| Integrals |  |
| Powers | $\begin{aligned} & \int x^{n} d x=\frac{x^{n+1}}{n+1} \\ & \int \frac{1}{x} d x=\ln x \end{aligned}$ |
| Exponentials | $\int e^{a x} d x=\frac{1}{a} e^{a x}$ |
| Trigonometry | $\begin{aligned} & \int \sin a x d x=-\frac{1}{a} \cos a x, \\ & \int \cos a x d x=\frac{1}{a} \sin a x \end{aligned}$ |
| Trigonometry |  |
| General | $\begin{aligned} & \sin \theta / \cos \theta=\tan \theta \\ & \sin ^{2} \theta+\cos ^{2} \theta=1 \end{aligned}$ |
| Two angles | $\sin (\alpha \pm \beta)=\sin \alpha \cos \beta \pm \sin \beta \cos \alpha$, $\cos (\alpha \pm \beta)=\cos \alpha \cos \beta \mp \sin \alpha \sin \beta$ |
| Double angles | $\begin{aligned} & \sin 2 \theta=2 \sin \theta \cos \theta \\ & \cos 2 \theta=\cos ^{2} \theta-\sin ^{2} \theta \end{aligned}$ |
| Logarithms |  |
| General | $\begin{aligned} & \ln a+\ln b=\ln (a b) \\ & \ln a-\ln b=\ln (a / b) \end{aligned}$ |

